

Acquiring and validating background knowledge for machine learning using function decomposition

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Abstract

Domain or background knowledge is often needed in order to solve difficult problems of learning medical diagnostic rules. Earlier experiments have demonstrated the utility of background knowledge when learning rules for early diagnosis of rheumatic diseases. A particular form of background knowledge comprising typical co-occurrences of several groups of attributes was provided by a medical expert. This paper explores the possibility to automate the process of acquiring background knowledge of this kind. A method based on function decomposition is proposed that identifies typical co-occurrences for a given set of attributes. The method is evaluated by comparing the typical co-occurrences it identifies, as well as their contribution to the performance of machine learning algorithms, to the ones provided by a medical expert.

Keywords

background knowledge

knowledge acquisition and validation

inductive learning

typical co-occurrences

function decomposition

diagnosis of rheumatic diseases

1 Introduction

When applying machine learning to learn medical diagnostic rules from patient records, it may be desirable to augment the latter with additional diagnostic knowledge about the particular domain, especially for difficult diagnostic problems. In machine learning terminology, additional expert knowledge is usually referred to as *background knowledge*. While most machine learning approaches have only limited capabilities of taking into account such knowledge, inductive logic programming [14] systems can handle different types of background knowledge.

A particular type of medical expert knowledge specifies which combinations of values (co-occurrences) of a set (grouping) of attributes have high importance for the diagnostic problem at hand. These combinations of values are called typical co-occurrences. A medical expert would specify the groupings as well as the typical co-occurrences associated with them.

Typical co-occurrences are used in expert diagnosis. When asked for some additional knowledge about the difficult problem of early diagnosis of rheumatic diseases, a medical expert provided typical co-occurrences for several groupings of attributes. These were then used by the LINUS [14] system for inductive logic programming in the domain of early diagnosis of rheumatic diseases [13] from anamnestic data. In this domain, the task is to diagnose patients into one of eight diagnostic classes, given sixteen anamnestic attributes. The difficulty of the diagnostic problem itself and noise in the data make this a very hard problem for machine learning approaches. A more detailed description of the domain can be found in Section 3.

The medical expert provided six groupings (pairs or triples of attributes) and their typical co-occurrences (characteristic combinations of values). These are given in Table 4 in Section 3. For each grouping, LINUS introduces a new attribute which is considered in the learning process. For a particular patient record (example) this attribute has as value the typical co-occurrence observed for the patient, if one was

indeed observed, or has the value “irrelevant” otherwise. A rule induction system, such as CN2 [3], or any attribute-value learning system can then be applied to the extended learning problem.

To illustrate the concept, let us consider Grouping 2. It relates the attributes “Spinal pain” and “Duration of morning stiffness” and the typical co-occurrences are: no spinal pain and morning stiffness up to 1 hour, spondylotic pain and morning stiffness up to 1 hour, spondylitic pain and morning stiffness longer than 1 hour. An example rule that uses this grouping and the second co-occurrence is given in Table 1. This rule was induced by LINUS using CN2 [13].

[Table 1 about here.]

The background knowledge in the form of typical co-occurrences was shown to have positive effect on rule induction in several respects. First, rules induced in the presence of background knowledge perform better in terms of classification accuracy and information content [13]. Second, it substantially improves the quality of induced rules from a medical point of view as assessed by a medical expert [13]. Finally, it reduces the effects of noisy data on the process of rule induction and nearest neighbor classification [7].

The motivation for our work is based on the following line of reasoning: It is very desirable to have and use background knowledge in the form of typical co-occurrences in rule induction, as it can greatly improve performance. Typical co-occurrences are also a natural and useful human concept used by the medical expert. However, it is well-known that direct knowledge acquisition from experts is an arduous and error-prone process [9]. This paper therefore proposes a method for automated acquisition of background knowledge in the form of typical co-occurrences. The expert need only specify the groupings, while the associated co-occurrences are determined automatically.

Before proceeding further, let us briefly mention related work. The domain of early diagnosis of rheumatic diseases has been first treated with a machine learning approach by Pirnat et al. [16]. Decision tree based approaches have been further applied to this domain by Karalič and Pirnat [10]. The use of background knowledge in this domain has been investigated by Lavrač et al. in combination with a decision tree approach [12] and in combination with a rule induction approach [13] and by Džeroski and Lavrač [7] in combination with nearest neighbor classification.

The typical co-occurrence acquisition method proposed in this paper uses several fundamental algorithms from function decomposition. The pioneers of this field are Ashenurst [1] and Curtis [5]. They have used function decomposition for the discovery of Boolean functions. Its potential use within machine learning was first observed by Samuel [17] and Biermann [2]. A recent report of Perkowski et al. [15] provides a comprehensive survey of the literature on function decomposition. In this paper we refer to the decomposition algorithms which use decision tables with multi-valued attributes and classes and were developed by Zupan et al. [20].

The remainder of the paper is organized as follows. Section 2 describes the method for acquisition of typical co-occurrences. Section 3 describes the domain of early diagnosis of rheumatic diseases, and the background knowledge provided by the expert. Taking the groupings provided by the expert, we apply the proposed method to determine the typical co-occurrences. The results of these experiments are also discussed in Section 3. Section 4 proposes a method for assisting the domain expert in selection of attribute groupings. Section 5 concludes and outlines some directions for further work.

2 The method

This section formally and through an example introduces the method that, given a set of examples represented as attribute-value vectors with assigned classes, derives

typical co-occurrences for a given set of attributes. The overall data-flow of the method is shown in Figure 1. The method first converts the set of examples to a decision table (Step 1). Next, decision table decomposition methods are used to derive a so-called partition matrix (Step 2). Finally, the typical co-occurrences for a given set of attributes are derived (Step 3), using an approach based on coloring the incompatibility graph of the partition matrix.

We first give an example of decision table decomposition and introduce the required decomposition methodology. The description of the method to acquire a set of typical co-occurrences is given next. For machine learning in medical domains, the data is usually represented as a set of examples, and we propose a technique to convert this representation to a decision table, a representation required by the proposed method. The section concludes with a brief note about the implementation.

[Figure 1 about here.]

2.1 Decision table decomposition: An example

Suppose we are given a *decision table* $y = F(X) = F(x_1, x_2, x_3)$ (Table 2) with three attributes x_1 , x_2 , and x_3 , and class y , and we want to decompose it to decision tables G and H , such that $y = G(x_1, c)$ and $c = H(x_2, x_3)$. For this decomposition, an initial set of attributes X is partitioned to a *bound set* $\{x_2, x_3\}$ used with H and a *free set* $\{x_1\}$ used with G . Decomposition requires the introduction of a new attribute c which depends only on the variables in the bound set.

[Table 2 about here.]

To derive G and H from F , we first need to represent a decision table with a *partition matrix* (Table 3). A partition matrix uses all possible combinations of attribute values from the bound set as column labels and those from the free set as

row labels. Each column in a partition matrix specifies a behavior of the function F when the attributes in the bound set are constant. Two elements of a partition matrix are compatible if they are the same or at least one of them is unknown (denoted by “-”). Two columns are compatible if all of their elements are pairwise compatible: these columns are considered to represent the same behavior of the function F .

[Table 3 about here.]

The problem is now to assign labels to the columns of the partition matrix so that only groups of mutually compatible columns have the same label. Columns with the same label exhibit the same behavior in respect to F and can use a single value of the new concept c . Label assignment involves the construction of a *column incompatibility graph*, where columns of the partition matrix are nodes and two nodes are connected if they are incompatible. Column labels are then assigned by coloring the incompatibility graph. For our example, the incompatibility graph with one of the possible optimal colorings is given in Figure 2.

[Figure 2 about here.]

For better comprehensibility, we interpret the column labels (colors) as follows: “1” as hi, “2” as med, and “3” as lo. These labels and the partition matrix straightforwardly determine the function $c = H(x_2, x_3)$. To determine the function $G(x_1, c)$, we lookup the annotated partition matrix for all the possible combinations of x_1 and c . The final result of the decomposition is represented as a hierarchy of two decision tables in Figure 3. If we further examine the discovered functions G and H we can see that $G \subset \text{MAX}$ and $H \subset \text{MIN}$.

[Figure 3 about here.]

2.2 Acquiring typical co-occurrences from a decision table

In the above example, different colors can be assigned to the same column of a partition matrix while retaining the minimal number of colors. For example, the column (med, lo) could be assigned either color 2 or 3, and the column (lo, hi) could be assigned any of the three colors used. On the other hand, the column (lo, lo) could only be assigned a single color because of the incompatibilities with (med, hi) and (hi, hi) which are assigned different colors. While there exists only one distinct behavior for (lo, lo) with respect to F , there exist several for (med, lo) and (lo, hi) . The combination (lo, lo) of attributes x_2 and x_3 thus tell us more about the behavior of the function F and is therefore more typical. Moreover, the columns that can be assigned only one color form a foundation for such color assignment and will be called *typical columns* of the partition matrix (*typical nodes* of the incompatibility graph) and will further indicate for *typical co-occurrences* of attributes in the bound set.

Therefore, for a given set of attributes for which we want to derive the typical co-occurrences (bound set) and for a given decision table, we have to first derive a corresponding partition matrix and its incompatibility graph. The algorithms for the construction of the partition matrix and incompatibility graph are described in detail in [20]. The typical co-occurrences derivation method then uses the incompatibility graph and discovers the typical co-occurrences through coloring. Since graph coloring is an NP-hard problem, the computation time of an exhaustive search algorithm is prohibitive even for small graphs with about 15 nodes. Instead, we use the simple Color Influence Method of polynomial complexity [15]. The Color Influence Method sorts the nodes to color by decreasing connectivity and then assigns to each node a color that is different from the colors of its neighbors so that a minimal number of colors is used. In this way, the coloring can have a single or several candidate colors for each node. The number of these candidate colors is used to determine the typicality of the node. We use the following definition:

Definition (Typical node n of incompatibility graph IG) *A node $n \in IG$ is typical if and only if in the process of coloring using the Color Influence Method it has only one candidate color to be assigned to.*

The above definition is then used to augment the Color Influence Method to both color the incompatibility graph and discover typical co-occurrences (Algorithm 1).

Input: incompatibility matrix IG

Output: typical co-occurrences for attributes in bound set

```

while there are no uncolored nodes in  $IG$  do
    select the uncolored node  $n \in IG$  with highest connectivity
    if there are no colored non-adjacent nodes
        or all colored non-adjacent nodes have the same color
    then  $n$  is typical else  $n$  is not typical endif
    color  $n$  with the first free color different from the colors of adjacent nodes
endwhile

```

Algorithm 1: Coloring of an incompatibility graph and selection of typical nodes

Let us illustrate the use of Algorithm 1 on the incompatibility graph from Figure 2. The nodes sorted by decreasing connectivity are

(hi,hi) , (med,hi) , (lo,lo) , (hi,lo) , (med,lo) , (lo,hi)

First, the node (hi,hi) is selected, determined to be typical (no other nodes have been colored yet), and assigned the color 1. Next, the node (med,hi) is considered. There are no colored nodes non-adjacent to it and so this node is typical. Since the adjacent node (hi,hi) has color 1, the color 2 is assigned to (med,hi) . Similarly, (lo,lo) is also typical and colored with 3 because the colors 1 and 2 have already been used for the adjacent nodes (hi,hi) and (med,hi) . Next, the node (hi,lo) has

a single colored non-adjacent node (lo, lo) and is thus typical and colored with the same color 3. The first non-typical node is (med, lo) : it has three nodes (med, hi) , (lo, lo) , and (hi, lo) that are non-adjacent to it and use different colors 2 and 3. Among these, the color 3 is then arbitrarily chosen for (med, lo) . Similarly, the node (lo, hi) is found not to be typical and among three candidate colors the color 3 is arbitrarily assigned to it. Therefore, among six possible combinations of attribute values the algorithm found four typical co-occurrences: (hi, hi) , (med, hi) , (lo, lo) , and (hi, lo) .

The described method finds a possible set of typical nodes but it does not guarantee that this is the only such set. An alternative method that would search more exhaustively and possibly evaluate all different coloring of the incompatibility graph may be more complete and propose different sets of typical co-occurrences, but its (possibly exponential) complexity would limit its applicability.

2.3 Derivation of a decision table from a set of examples

The typical co-occurrence derivation method requires domain data in the form of a decision table. Decision tables require nominal attributes and for a specific combination of attribute values define at most one class. However, the data sets from medical domains often include continuous attributes and may use several examples with the same attribute values but possibly different classes. Therefore, we need a method that, given a set of domain examples, would derive a corresponding decision table. For all continuous attributes, we assume that a discretization is given or can be derived from the examples.

The method is given in Algorithm 2. It searches through the set of examples E whose attribute values are the same if nominal or discretize to the same value if continuous. For such sets of examples E' , a majority class value is found and a corresponding entry is added to the decision table. The examples from E' are then

removed from E and the process repeated until there are no more examples in E .

Input: Set of examples $E = \{e_i\}$, Discretization for continuous attributes
Output: Decision table DT

while $E \neq \emptyset$ **do**
 select $e_j \in E$
 find $E' = \{e_k; e_k \in E\}$ such that
 1) for all discrete attributes, e_k has the same value as e_j
 2) for all continuous attributes, e_k 's discretized value is the same as e_j 's
 $E' \leftarrow E' \cup \{e_j\}$
 $c \leftarrow$ a majority class value of examples in E'
 add e_j with discretized continuous values and with class c to DT
 $E \leftarrow E \setminus E'$
endwhile

Algorithm 2: Derivation of a decision table from a set of examples

2.4 Implementation

The typical co-occurrences extraction method was implemented as HINT_{TCO} , an extension of the Hierarchy Induction Tool HINT [20] for learning concept hierarchies from examples by decision table decomposition. Both HINT and HINT_{TCO} run on a variety of UNIX platforms, including HP/UX, SunOS and IRIS.

3 Extraction and validation of typical co-occurrences in early diagnosis of rheumatic diseases

3.1 The domain

The data on early diagnosis of rheumatic diseases used in our experiments originate from the University Medical Center in Ljubljana [16] and comprise records on 462 patients. The multitude of over 200 different diagnoses have been grouped into three, six, eight or twelve diagnostic classes. Our study uses eight diagnostic classes: degenerative spine diseases, degenerative joint diseases, inflammatory spine diseases, other inflammatory diseases, extraarticular rheumatism, crystal-induced synovitis, non-specific rheumatic manifestations, and non-rheumatic diseases.

For each patient, sixteen anamnestic attributes are recorded: sex, age, family anamnesis, duration of present symptoms (in weeks), duration of rheumatic diseases (in weeks), joint pain (arthrotic, arthritic), number of painful joints, number of swollen joints, spinal pain (spondylotic, spondylitic), other pain (headache, pain in muscles, thorax, abdomen, heels), duration of morning stiffness (in hours), skin manifestations, mucosal manifestations, eye manifestations, other manifestations, and therapy. The continuous attributes (age, durations and numbers of joints) have been discretized according to expert suggestions. For the continuous attributes that appear in groupings, the discretizations can be read out from Table 4. For example, from Table 4.1 we can see that the attribute “Duration of morning stiffness” has been discretized into two intervals: up to 1 hour and longer than 1 hour.

3.2 The background knowledge

In an earlier study [12], a specialist for rheumatic diseases has provided his knowledge about typical co-occurrences of six groupings of attributes. The groupings and

the co-occurrences are given in Table 4, where a bullet in the column marked “specialist” and the row marked X means that tuple X is a typical co-occurrence for the corresponding Grouping. For example, Table 4.1 specifies Grouping 1, which relates the attributes “Joint pain” and “Duration of morning stiffness”, with typical co-occurrences suggested by HINT_{TCO} : no joint pain and morning stiffness up to 1 hour, arthrotic pain and morning stiffness up to 1 hour, arthritic pain and morning stiffness up to 1 hour.

3.3 The experiments

To evaluate our method for typical co-occurrences acquisition, we took the dataset and the six groupings described above, the latter without the typical co-occurrences provided by the expert. We then applied our method to produce the typical co-occurrences. For each grouping, the typical co-occurrences produced by HINT_{TCO} are listed in the column labeled “ HINT_{TCO} ” of the corresponding table. For example, HINT_{TCO} suggests that the typical co-occurrences for Grouping 1 should be: no joint pain and morning stiffness up to 1 hour, arthrotic pain and morning stiffness up to 1 hour, arthritic pain and morning stiffness up to 1 hour.

The groupings with the new typical co-occurrences suggested by HINT_{TCO} are then provided as background knowledge to LINUS [14] in addition to the 462 training examples (patient records). LINUS then introduces a new attribute for each grouping (as explained in the introduction). The 462 examples augmented with the six new attributes (thus having in total 22 attributes) are then fed to the rule induction system CN2 [3] and to a nearest neighbor classifier [19, 8, 4]. The goal of this was to evaluate the usefulness of the new attributes and in this way the usefulness of the typical co-occurrences proposed by HINT_{TCO} .

The number of occurrences of each grouping (i.e., the new attribute corresponding to that grouping) in the set of rules induced by CN2 is listed in the column

marked f_{CN2} . The mutual information between the grouping and the diagnostic class, calculated as a weight for nearest neighbor classification [19] is listed in the column marked f_{NN} . The mutual information [18] between an attribute and the class tells us how useful the attribute is for classification. The two measures have been used in earlier experiments to assess the utility of background knowledge in machine learning [13, 7].

[Table 4 about here.]

3.4 The results

For groupings 1, 2, 5, and 6, the typical co-occurrences derived by HINT_{TCO} correspond reasonably well to those proposed by the specialist for rheumatic diseases. For these groups, while using the same (groupings 1, 2, and 6) or slightly higher number of co-occurrences (grouping 5), two thirds or more of the co-occurrences originally proposed by the specialist were discovered by HINT_{TCO} . This is different to grouping 4, where less than one half of the co-occurrences match and to grouping 3, where there are no matches.

In terms of the mutual information evaluation metrics f_{NN} , the co-occurrences derived by HINT_{TCO} score higher for all but the grouping 4. A similar behavior is observed when the number of appearances in CN2 induced rules f_{CN2} is used as an evaluation metrics. There, HINT_{TCO} scores equal or higher for all but the groupings 1 and 4.

Overall, compared to the co-occurrences proposed by the specialist, HINT_{TCO} performed well for groupings 1, 2, 5, and 6. There are slight differences in the proposed co-occurrences, which, in turn, contribute to higher values of the evaluation metrics. For grouping 3, there is a complete mismatch between the co-occurrences proposed by the specialist and those derived by HINT_{TCO} . The co-occurrences derived by

HINT_{TCO} score higher on both metrics (4 to 1 on f_{CN2}). However, the weights assigned by mutual information suggest that this grouping might be substantially less important for classification than the others (f_{CN2} of 0.096 and 0.080).

It is grouping 4 where the of co-occurrences derived by HINT_{TCO} seem to be less appropriate than those proposed by the specialist. However, note that for this grouping the specialist proposed six co-occurrences while HINT_{TCO} discovered only four. Instead of using HINT_{TCO} to derive only the typical co-occurrences for which the corresponding number of colors in the partition matrix is one, we can use this number as a measure of appropriateness for a certain combination of attribute values to be used as a typical co-occurrences. The lower the number of colors, the better the corresponding combination. For grouping 4, the number of possible colors for the columns in the partition matrix is shown in Table 5. It indicates that (No pain, Spondylotic) and (No pain, Spondylitic) are the next best candidates for typical co-occurrences. Interestingly, both are also proposed by the specialist. Their inclusion to the set of typical co-occurrences derived by HINT_{TCO} makes this set very similar to that of the specialist, and also increases the mutual information weight from 0.743 to 0.887.

[Table 5 about here.]

With the above extension, we can therefore conclude that HINT_{TCO} discovered typical co-occurrences that were comparable to those proposed by the expert both in terms of similarity and usefulness as background knowledge for machine learning. This is important since HINT_{TCO} is not meant to be a stand-alone tool for unsupervised discovery of background knowledge, but should rather provide support to the expert by (1) proposing a set of co-occurrences and (2) weighting different combinations of attribute values to indicate how important it is that they are included in such a set. It would then be up to the expert to decide which of the proposed co-occurrences are meaningful and should be used.

As an overall evaluation of the typical co-occurrences suggested by HINT_{TCO} , let us consider the performance and size of the rules induced by CN2 from the dataset generated by LINUS. The performance measures used were the accuracy and information content [11, 6] (as measured on the training set) of the rules induced (using the significance test in CN2). Also observed were the total number of rules induced and the number of rule conditions used. The results (Table 6) indicate that both the accuracy and information content are higher when LINUS uses background knowledge in the form of typical co-occurrences. Moreover, while typical co-occurrences as proposed by HINT_{TCO} yield rules of higher accuracy and slightly higher information content than rules obtained when expert defined co-occurrences are used, they also result in a less complex classifier in terms of number of rules and their conditions.

[Table 6 about here.]

4 Computer-assisted selection of attribute groupings

In the experiments described above HINT_{TCO} assumed the set of attributes for which to derive typical co-occurrences were given in advance. A possible extension of this approach is to propose not only co-occurrences but also the set of attributes for which the background knowledge in the form of co-occurrences should be defined. The idea is straightforward and is illustrated with Algorithm 3. The algorithm examines all groupings of attributes from a candidate set (e.g., all pairs and triples) and for each grouping derives the set of typical co-occurrences. Each grouping is then assigned a weight, which estimates the usefulness of the grouping for the classification. The groupings, sorted by decreasing weight, are then presented to the user who decides which of the proposed groupings are meaningful and are in his opinion suitable for use as background knowledge.

Input: set of examples

Output: sorted list of attribute groupings with assigned weights

derive a decision table from the set of examples

for all the pairs (and triples) of attributes **do**

 derive the typical co-occurrences

 derive the corresponding weight

endfor

sort the groupings by descending weights and present them to the user

Algorithm 3: Derivation of groups of (two and three) attributes for which background knowledge in the form of typical co-occurrences might be useful for machine learning

We have used this idea to obtain a list of sorted groupings of two attributes for the data on early diagnosis of rheumatic diseases. The groupings were ranked according to the mutual information [18] between an attribute obtained from grouping and the diagnostic class. While all five two-attributes grouping from Table 4 originally proposed by the expert ranked in the upper half of the sorted list of groupings, the Grouping 4 and Grouping 2 were ranked within the best six groupings, which were:

1. “Spinal pain” and “Swollen joints”
2. “Number of painful joints” and “Spinal pain”
3. “Spinal pain” and “Skin manifestations”
4. “Joint pain” and “Spinal pain” (Grouping 4)
5. “Spinal pain” and “Therapy”
6. “Spinal pain” and “Morning stiffness” (Grouping 2)

Note that six highest ranked all include “Spinal pain”. This may be contributed to by the high mutual information between this attribute and class itself, which is also the highest of all nominal attributes used in the rheumatic diseases dataset.

For an additional experiment, we have used the six groupings above and their typical co-occurrences as proposed by HINT_{TCO} for background knowledge, which was then used by LINUS. The corresponding CN2 induced rules had an information content of 30% and classification accuracy of 51.2%. While the information content is similar to that when groupings are proposed by expert, the classification accuracy is lower. This indicates that the involvement of an expert in the selection of groupings may not only have a positive effect on the comprehensibility of rules, but also on their classification performance.

5 Conclusions

Background knowledge in the form of typical co-occurrences has positive effect on machine learning results in terms of the performance and the quality of induced rules from a medical point of view. We have developed a method that proposes typical co-occurrences through functional decomposition of a given set of examples. While medical diagnosis background knowledge of this type has been previously completely specified by a medical expert, our approach offers the possibility to automate the background knowledge acquisition process by proposing typical co-occurrences to the expert, who would then consider them in the light of his expert knowledge.

Experiments indicate that the use of typical co-occurrences identified by our method improves the performance of machine learning as compared to the use of typical co-occurrences provided by a medical expert. While potentially useful attribute groupings can also be identified automatically, experiments indicate that expert involvement in the selection process is probably necessary to achieve high performance.

For further work, a more careful evaluation of the background knowledge acquired through using our method is needed. This should include an evaluation of the quality of induced rules from a medical point of view. An evaluation of the performance in terms of classification accuracy on unseen cases is also desirable, but requires a

slightly more complicated experimental setup: typical co-occurrences would have to be determined for each partition of the dataset into training and testing cases. Finally, experiments with an active involvement of a domain expert in both attribute grouping and typical co-occurrence selection should be conducted.

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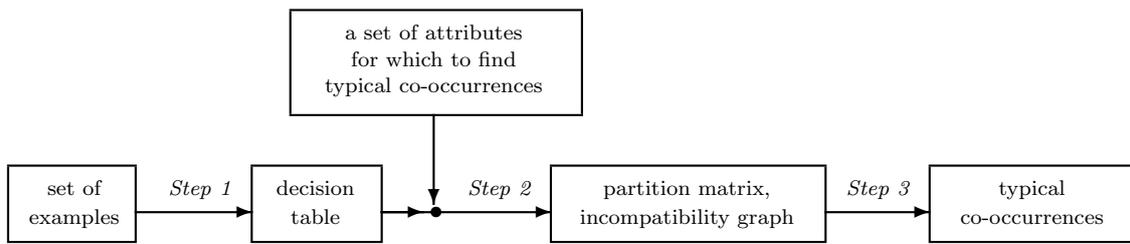


Figure 1:

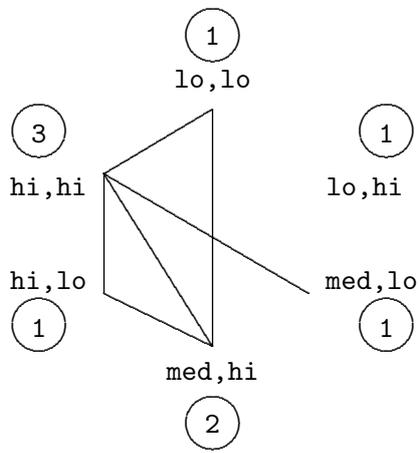


Figure 2:

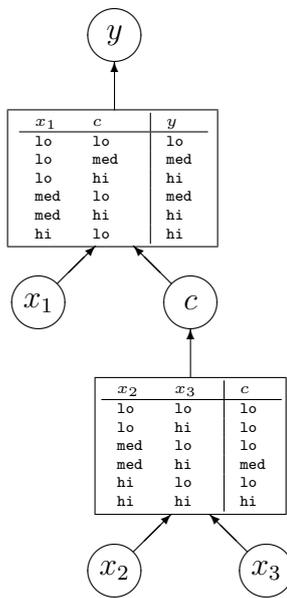


Figure 3:

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Table 1:

```
IF   Duration_of_present_symptoms > 6.5 months
AND  Duration_of_rheumatic_diseases < 5.5 years
AND  Number_of_painful_joints > 16
AND  grouping2(Spinal_pain,Duration_of_morning_stiffness) =
      'spondylotic & up to 1 hour'
THEN Diagnosis = Degenerative_spine_diseases
```

Table 2:

x_1	x_2	x_3	y
lo	lo	lo	lo
lo	med	hi	med
lo	hi	lo	lo
lo	hi	hi	hi
med	med	lo	med
med	hi	lo	med
med	hi	hi	hi
hi	lo	lo	hi
hi	hi	lo	hi

Table 3:

	x_2	lo	lo	med	med	hi	hi
x_1	x_3	lo	hi	lo	hi	lo	hi
lo		lo	-	-	med	lo	hi
med		-	-	med	-	med	hi
hi		hi	-	-	-	hi	-
color		3	3	3	2	3	1

Table 4:

Joint pain, Morning stiffness	specialist	HINT _{TCO}
No pain, ≤ 1 hour	•	•
Arthrotic, ≤ 1 hour	•	•
Arthritic, ≤ 1 hour		•
No pain, > 1 hour		
Arthrotic, > 1 hour		
Arthritic, > 1 hour	•	
f_{CN2}	2	1
f_{NN}	0.345	0.353

1)

Spinal pain, Morning stiffness	specialist	HINT _{TCO}
No pain, ≤ 1 hour	•	•
Spondylotic, ≤ 1 hour	•	•
Spondylitic, ≤ 1 hour		•
No pain, > 1 hour		
Spondylotic, > 1 hour		
Spondylitic, > 1 hour	•	
f_{CN2}	3	3
f_{NN}	0.545	0.643

2)

Sex, Other pain	specialist	HINT _{TCO}
male, no		•
male, muscles		•
male, thorax	•	
male, heels	•	
male, other		•
female, no		•
female, other		•
other 7 combinations		
f_{CN2}	1	4
f_{NN}	0.080	0.096

3)

Joint pain, Spinal pain	specialist	HINT _{TCO}
No pain, No pain	•	•
Arthrotic, No pain	•	•
Arthritic, No pain	•	•
No pain, Spondylotic	•	
Arthrotic, Spondylotic		•
Arthritic, Spondylotic		
No pain, Spondylitic	•	
Arthrotic, Spondylitic		
Arthritic, Spondylitic	•	
f_{CN2}	9	8
f_{NN}	0.908	0.743

4)

Joint pain, Spinal pain, Painful joints	specialist	HINT _{TCO}
No pain, No Pain, 0	•	•
No pain, No Pain, 1 ≤ joints ≤ 5		•
No pain, Spondylotic, 0	•	•
No pain, Spondylitic, 0	•	•
Arthrotic, No pain, 1 ≤ joints ≤ 5	•	•
Arthrotic, No pain, 5 < joints ≤ 30	•	•
Arthrotic, Spondylotic, 1 ≤ joints ≤ 5		•
Arthrotic, Spondylitic, 5 < joints ≤ 30		•
Arthritic, No pain, 1 ≤ joints ≤ 5	•	•
Arthritic, No pain, 5 < joints ≤ 30	•	•
Arthritic, Spondylitic, 1 ≤ joints ≤ 5	•	
other 25 combinations		
f_{CN2}	7	9
f_{NN}	0.757	0.834

5)

Swollen joints, Painful joints	specialist	HINT _{TCO}
0, 0	•	•
0, 1 ≤ joints ≤ 5	•	•
0, 5 < joints ≤ 30	•	
0, 30 <		•
1 ≤ joints ≤ 10, 0	•	•
1 ≤ joints ≤ 10, 1 ≤ joints ≤ 5	•	
1 ≤ joints ≤ 10, 5 < joints ≤ 30	•	•
1 ≤ joints ≤ 10, 30 <		
10 <, 0		
10 < 1 ≤ joints ≤ 5,		
10 <, 5 < joints ≤ 30		
10 <, 30 <		
f_{CN2}	1	1
f_{NN}	0.331	0.392

6)

Table 5:

Joint pain, Spinal pain	# colors
No pain, No pain	1
Arthrotic, No pain	1
Arthritic, No pain	1
No pain, Spondylotic	2
Arthrotic, Spondylotic	1
Arthritic, Spondylotic	3
No pain, Spondylitic	2
Arthrotic, Spondylitic	3
Arthritic, Spondylitic	4

Table 6:

	Accuracy	Inf. content	# Rules	# Conditions
w/o background knowledge	51.7%	22%	30	102
co-occurrences by expert	52.4%	30%	38	120
co-occurrences by HINT_{TCO}	56.5%	31%	35	106